

Making Sense of (Multi-)Relational Data

Part II: Exploration through targeted patterns





Approaches

• Safarii / "Multi-Relational Data Mining"

• RDB-Krimp

• Inductive Logic Programming





Safarii / "Multi-Relational Data Mining"





Data

• Relational database / E-R model

Molecule				
id	name			
1	CO ₂			
2	H ₂ O			

Atom							
id	mol_id	element					
1	1	С					
2	1	0					
3	1	0					
4	2	Н					
5	2	Н					
6	2	0					

Knobbe (2004)

Bond						
id	atom1	atom2	type			
1	1	2	double			
2	1	3	double			
3	4	6	single			
4	5	6	single			

Figure 3.2 Relational representation of CO₂ and H₂O.



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Data

• Relational database / E-R model



Knobbe (2004)



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Example pattern

Pattern =

 all molecules with
 at least one bond
 and a C atom





Pattern syntax

- Individuals are records in the target table, along with its associations and associated parts
 - The units which we want to predict/describe

• A *subgroup* is a set of individuals



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Pattern syntax

• Pattern = subgroup = selection graphs







Pattern syntax

• Pattern = subgroup = selection graphs

- Mining is then *refinement* of selection graphs
 - Conditioning: choose subset of values (=, ≥, ≤)
 - Association: add an association



Pattern syntax

• Simple case: condition & association refinement





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Knobbe (2004)

Figure 3.2 Relational representation of CO₂ and H₂O.



Implementation of MRDM: Safarii

• Relational association rule discovery

- Find refinements using aggregation
 - Categorical: select an attribute-value
 - Numerical: exists $\leq \geq$, min \leq , max \geq
 - These are SQL primaries, there are many more possibilities



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Algorithmic approach

- Restrict # associations, # refinements
- Generate SQL queries, push workload to DB

- Aggregation is greedy
 - Choose only optimal split at runtime
 - Essentially a form of *local discretisation*



Knobbe (2004)

Algorithmic approach

• Patterns are also SQL queries



FROM molecule T0, bond T1, atom T2
WHERE T0.id = T1.molecule_id and T0.id = T2.molecule_id
AND T2.element = 'C'

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Interestingness

- Several objective interestingness measures
 - support(S \rightarrow T) = P(ST)
 - coverage(S \rightarrow T) = P(S)
 - accuracy(S \rightarrow T) = P(T|S)
 - specificity(S \rightarrow T) = P(\neg S $|\neg$ T)
 - sensitivity($S \rightarrow T$) = P($S \mid T$)
 - novelty(S \rightarrow T) = P(ST) P(S)·P(T)



Interestingness

• Several objective interestingness measures

• Steer aggregation

• Rank rules







RDB-Krimp





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Data

- Relational database / E-R model
- Table defined as: key, foreign keys, attributes
 - Categorical attributes only



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Sept 11, 2015

Koopman & Siebes (2009)

T ⁱ					
K ⁱ	F ⁱ j	A ⁱ 1	A ⁱ 2		
k	ı kj	I V1	I V2		

T ¹ = ACCOUNT						
account _{ID} Frequency Date						
10	2	06/2007				
11	3	03/2006				
12	3	08/2006				
13	2	03/2006				
14	1	05/2008				

$T^2 = LOAN$							
loan _{ID}	account _{ID}	Date	Amount	Duration	Payment		
30	ı 10	06/2008	10245	12	A		
31	10	09/2008	13722	24	В		
32	11 II	08/2006	27313	36	В		
33	12	09/2006	27147	12	В		
34	12	05/2008	27194	36	D		
35	13	09/2008	ı 30289	ı 12	I B		
36	13	06/2008	18203	12	С		

$T^3 = ORDER$							
ordern _{ID}	account _{ID}	Bank-To	Amount-To	Amount	Туре		
20	i 10	i ST	141	1000	UVER		
21	l 10	l QR	359	2000	SIPO		
22	, 11	ı YZ	850	1000	SIPO		
23	I 13	I ST	283	1000	NULL		
24	13	I OP	850	2000	SIPO		

$T^4 = DISPOSITION$							
disp_{ID} account _{ID} Type							
40	10	I OWNER					
41	11	DISPONENT					
42	11	OWNER					
43	I 12	DISPONENT					
44	12	OWNER					

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Pattern syntax

• Given a target table *T* with key *K*

• Pattern =

selection of attribute values (conj + disj) of T
& selection of attribute values (conj + disj) for
tables with K as foreign key



P₁:ACCOUNT({ Frequency = 2 })

- [[ORDER({ Bank-To=ST, Amount=1000 }),
 - ORDER({ Amount=2000, Type=SIPO })] ,
- [[LOAN({ Date='06/2008', Duration=12 }), LOAN({ Date='09/2008', Payment=B })]]

frequency(
$$P_1$$
) = 2, count(P_1) = 10, size(P_1) = 9

P₂: ACCOUNT({ Frequency = 3 }) [[DISPOSITION({ Type = Disponent }), DISPOSITION({ Type = Owner })]]

Koopman &

frequency(P_2) = 2, count(P_2) = 6, size(P_2)=3

Partially Covered Database

T ¹ = ACCOUNT			$T^2 = LOAN$						
account _{ID}	Frequency	Date	loan _{ID}	account _{ID}	Date	Amount	Duration	Payment	
10	2//	06/2007	30	i 10	06/2008	10245	í / 12 /	A	
11	3	03/2006	31	l 10	09/2008	13722	24	<u> </u>	
12	3	08/2006	32	, 11	08/2006	27313	36	, I В	
13	2//	03/2006	33	I 12	09/2006	27147	12	I B	
14	1	05/2008	34	12	05/2008	27194	36	D	
15	1 3	03/2006	36	1 13	06/2008	18203	1/1/2/	I C]∢
16	2	06/2007	35	13	09/2008	30289	12	B	∢

	$T^3 = ORDER$						
ordern _{ID}	account _{ID}	Bank-To	Amount-To	Amount	Туре		
20	i 10	i / s 7 / i	141	1000	UVER		
21	1 10	QR	359	/2000/ /	Sípo /		
22	, 11	YZ	850	1000	SIPO		
23	l 13	/ST/	283	1000	NULL		
24	13	OP	850	2000	/SIPO//		

$T^4 = DISPOSITION$						
disp _{ID}	account _{ID}	Туре				
40	i 10	I OWNER				
41	11	DISPONENT				
42	, 11	OWNER				
43	I 12	DISPONENT				
44	12	OWNER				



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Algorithmic (enumeration) approach

• Run FARMER for every table in DB as target

• FARMER (Nijssen & Kok, 2003) is an ILP algorithm for enumeration of frequent 'queries'

• Exhaustive search with *minsup* threshold



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Interestingness

• Main contribution of RDB-Krimp

- Find **concise** set of local patterns that together describe the DB well
 - → Minimum Description Length principle
 - Two part code L(H) + L(D|H)



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Interestingness

- Greedy approximation algorithm:
- 1. Initialise pattern set as all singletons
- 2. Try insert patterns one by one
 - Keep if total description length decreases
- No guarantees on optimality



Koopman & Siebes (2009)

Sept 11, 2015





Inductive Logic Programming





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(Probabilistic) Inductive Logic Programming

- Field of research
 - Also related to / equivalent with probabilistic logic learning, statistical relational learning, logical and relational learning
- Ultra brief review
 - We are not experts
 - Too much to cover



Data

- Logical representation
 - Also an E-R model ?





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Pattern syntax

- Generalises all pattern mining syntaxes discussed here
- Can derive predicates (rules)
 - Can have no antecedent \rightarrow association but not 'rule'
 - Terms can be variables rather than constants daughter(C, P) :- female(C), mother(P, C)

[De Raedt & Kersting, 2008]



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Algorithmic approach

- Very different terminology
 - Logic, but
 - Various frameworks (entailment, interpretations, proofs)
- Also based on 'generality' (= monotonicity)
- Search can easily become very costly



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Interestingness

- Objective interestingness measures have been employed
 - Frequency
 - Confidence



De Raedt (2008) Case I: Structure Activity Relationship Prediction



[Srinivasan et al.AlJ 96]

Structural alert:



General Purpose Logic Learning System

Uses and Produces Knowledge

Data = Set of Small Graphs



De Raedt (2007)

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Dehaspe's Warmr ~ Apriori

PARTICIPANT Table							
NAME	JOB	COMPANY	PARTY	R_NUMBER			
adams	researcher	scuf	no	23			
blake	president	j∨t	yes	5			
king	manager	ucro	no	78			
miller	manager	j∨t	yes	14			
scott	researcher	scuf	yes	94			
turner	researcher	ucro	no	81			

COMPANY Table		
COMPANY	TYPE	
j∨t	commercial	
scuf	university	
ucro	university	

COURSE Table		
COURSE	LENGTH	TYPE
CSO	2	introductory
erm	3	introductory
so2	4	introductory
srw	3	advanced

SUBSCRIPTION Table		
NAME	COURSE	
adams	erm	
adams	so2	
adams	srw	
blake	CSO	
blake	erm	
king	CSO	
king	erm	
king	so2	
king	srw	
miller	so2	
scott	erm	
scott	srw	
turner	so2	
turner	srw	

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